Multivariate Calculus

Estimating rate of change

The accompanying plot below shows constant temperature T (in Kelvin) level curves as given by the ideal gas law pV = nRT with n = 0.15 mol and R = 0.082 L·atm/(mol·K).

- 1. Use information from the plot to estimate the rate of change in temperature T with respect to change in volume V for V = 0.2 L and p = 0.2 atmospheres.
- 2. Use information from the plot to estimate the rate of change in temperature T with respect to change in pressure p for V = 0.2 L and p = 0.2 atmospheres.
- 3. Repeat Steps 1 and 2 for each of the following (V, p) pairs.

(a) (0.2 L, 0.4 atm) (b) (0.2 L, 0.6 atm) (c) (0.2 L, 0.8 atm)

(d)
$$(0.4 \text{ L}, 0.2 \text{ atm})$$
 (e) $(0.6 \text{ L}, 0.2 \text{ atm})$ (f) $(0.8 \text{ L}, 0.2 \text{ atm})$

- 4. Use your previous results to make a plot showing rate of change in temperature T with respect to volume V versus pressure p for V = 0.2 L.
- 5. Use your previous results to make a plot showing rate of change in temperature T with respect to volume V versus volume V for p = 0.2 atm.
- 6. Use your previous results to make a plot showing rate of change in temperature T with respect to pressure p versus pressure p for V = 0.2 L.
- 7. Use your previous results to make a plot showing rate of change in temperature T with respect to pressure p versus volume V for p = 0.2 atm.

