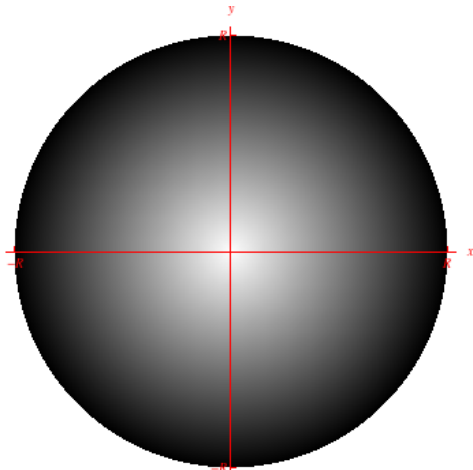


Total from area density

Problem: Charge is distributed on a disk of radius R so that the area charge density is proportional to the distance from the center, reaching a maximum value σ_0 at the far edge. Compute the total charge.



Total from area density

$$\begin{aligned}Q &= \iint_{\text{disk}} \sigma \, dA \\&= \int_a^b \int_c^d \sigma(x, y) \, dydx \\&= \int_{-R}^R \int_{-\sqrt{R^2-x^2}}^{\sqrt{R^2-x^2}} \sigma(x, y) \, dydx \\&= \int_{-R}^R \int_{-\sqrt{R^2-x^2}}^{\sqrt{R^2-x^2}} \frac{\sigma_0}{R} \sqrt{x^2 + y^2} \, dydx \\&= \text{not fun to evaluate}\end{aligned}$$

Turn to a different coordinate system: polar coordinates.