## Implicit differentiation example

A plot for the implicit relation $x^{3}+y^{2}+3 x y=0$ is shown below.


1. The curve has two points corresponding to $x=2$. Use the plot to estimate the $y$ coordinate for each of these points.
2. Substitute $x=2$ into the relation $x^{3}+y^{2}+3 x y=0$. Solve the resulting equation to find the exact values of the $y$ coordinate for each of these points.
3. Draw an estimated tangent line at each of the two points corresponding to $x=2$. Estimate the slope of each line you draw.
4. Use implicit differentiation to compute the derivative $\frac{d y}{d x}$.
5. Evaluate $\frac{d y}{d x}$ for each of the two points corresponding to $x=2$. Compare these values with the slopes you estimated in 3 .
