

Computing divergence and curl

1. Compute the divergence for each of the following vector fields.

(a) $\vec{F} = x \hat{i} + y \hat{j}$

(b) $\vec{F} = x \hat{i} + y \hat{j} + z \hat{k}$

(c) $\vec{F} = z \sin(xy) \hat{i} + (x + y) \hat{j} + ze^x \hat{k}$

(d) $\vec{F} = -y \hat{i} + x \hat{j}$

(e) $\vec{F} = \frac{x \hat{i} + y \hat{j}}{\sqrt{x^2 + y^2}}$

(f) $\vec{F} = \frac{x \hat{i} + y \hat{j}}{x^2 + y^2}$

2. Compute the curl for each of the following vector fields.

(a) $\vec{F} = x \hat{i} + y \hat{j}$

(b) $\vec{F} = x \hat{i} + y \hat{j} + z \hat{k}$

(c) $\vec{F} = z \sin(xy) \hat{i} + (x + y) \hat{j} + ze^x \hat{k}$

(d) $\vec{F} = -y \hat{i} + x \hat{j}$

(e) $\vec{F} = \frac{-y \hat{i} + x \hat{j}}{\sqrt{x^2 + y^2}}$

(f) $\vec{F} = \frac{-y \hat{i} + x \hat{j}}{x^2 + y^2}$