

February 25, 2000

Name

Technology used: _____

Textbook/Notes used: _____

Directions: Be sure to include in-line citations, including page numbers if appropriate, every time you use a text or notes or technology. Include a careful sketch of any graph obtained by technology in solving a problem. **Only write on one side of each page.**

The Problems

1. Use the definition (the limit form) of derivative to find $f'(x)$ if $f(x) = \frac{1}{2x+1}$.
2. Below is the graph of a function on a grid. Assuming the grid lines are spaces 1 unit apart both vertically and horizontally, sketch the graph of the derivative function over the same interval. Use the same

grid for your sketch.

3. State the definition of:
 - (a) A function f being continuous at $x = c$.
 - (b) A function f being differentiable at $x = c$.

4. Given the function $f(x) = \begin{cases} x^2 - 6, & x < 2 \\ -2, & x = 2 \\ Ax - 12, & x > 2 \end{cases}$

- (a) Determine, with explanation, a value of A that makes f continuous at $x = 2$ or explain why no such number A exists.
5. Do **one** of the following.

- (a) When working with the exponential function $f(x) = 3^x$, some people prefer to use the function $g(x) = e^{kx}$ where $k = \ln(3)$. Use logarithm and exponential rules to show these are really the same function.
- (b) Determine the **exact** values of each of the following.
- $\arcsin(1)$
 - $\arctan(1)$
 - $\cos(\arccos(\sqrt{2}/2))$
 - $\arcsin(\sin(12\pi))$ [Be careful.]
 - $\exp(3 \ln(4))$.

6. Do **one** of the following.

- (a) Without using a calculator, determine the following limits. Be sure to briefly justify your answer.
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$$\lim_{x \rightarrow 0} \frac{\sin^2(x)}{x}$$

ii.

$$\lim_{x \rightarrow 0} \frac{1}{1 + 3^x}$$

iii.

$$\lim_{x \rightarrow 2} \frac{x^2 + 5x - 14}{3x^2 - 3x - 6}$$

- (b) Without using a calculator, determine the following limits. Be sure to justify your answer.
-

$$\lim_{x \rightarrow 1^-} \frac{10}{1 + 2^{1/(x-1)}}$$

ii.

$$\lim_{x \rightarrow 0^+} \left(\frac{1}{x} - \frac{1}{x^2} \right) \text{ Hint: } \frac{\infty}{\infty} \text{ is a "be careful" (indeterminate) form.}$$